

Recent Advances in Deep Anomaly Detection

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This tutorial ...

- A short tutorial (50 min) to introduce brief ideas and some promising approaches
 - Not an exhaustive survey
- Focus on anomaly detection in computer vision and medical image analysis
 - You can find much literature on novelty detection in many domains
- Review of recent anomaly detection methods in 2017 ~ 2020



Outline

- Medical imaging and anomaly detection
 - Clinical motivation
 - Anomaly detection system
 - Anomaly score
 - Challenges in anomaly detection
- Anomaly detection approaches in computer vision and medical imaging
 - Deep learning based approaches
 - Unsupervised and hybrid methods
 - One-class neural networks
 - Medical applications
 - Anomaly scores for medical images
- Summary
 - Limitations and Challenges



Anomaly Detection

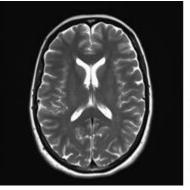
Medical Imaging Applications



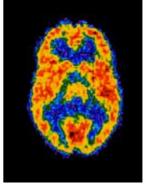
Medical Imaging

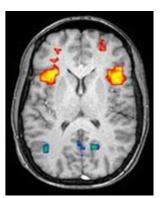
- "Process of creating visual representations of the interior of a body for clinical analysis and medical intervention"
 - Interpreted by medical doctors, radiologists or sonographers
 - For diagnostic purpose
- CT, MRI, ultrasound imaging, functional imaging, ...







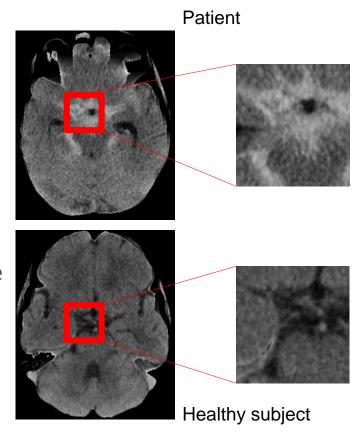






Brain Hemorrhage

- Diagnosis using medical images
 - Find any lesion
 - Compare and measure
- What can you see?
 - Same anatomical structure
 - Location and shape
 - Differences in pixel intensity and texture
 - Expansion of the structure?
 - Compared to healthy subject's image

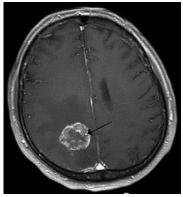


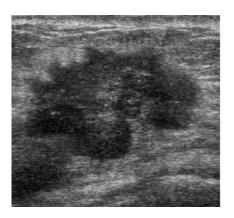


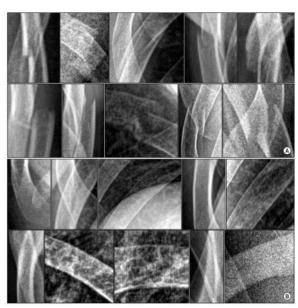
Anomalies in Medical Images

- Definition of anomaly
 - "A deviation from the common rule, type, arrangement, or form"
 - Also referred as abnormalities, outliers, or deviants
- Anomalies in diagnostic medical images
 - Uncommon patterns in images
 - How to detect and quantify





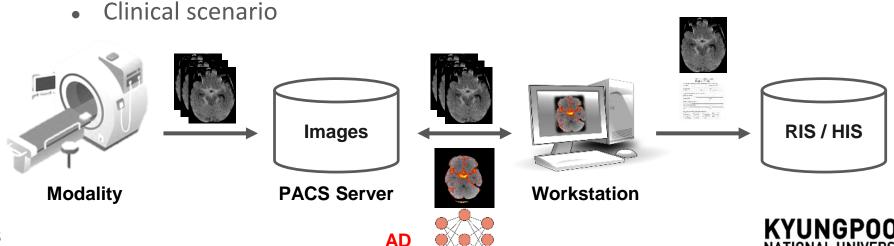






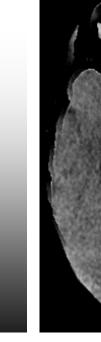
Anomaly Detection in Medical Imaging

- Early detection of lesions is critical
 - Better prognosis and able to prevent severe symptoms
- Problems in real world
 - Number of experienced doctors < number of patients and scans
 - Difficult to read all slices of 3D volumes → time-consuming
 - Dataset for possible anomalies → not available in most cases



Characteristics of Anomalies

- Brain Hemorrhage
 - Hounsfield unit
 - Different grey levels to hemorrhage
 - Distinguishable from surrounding structures and normal cases
- **Anomalies**
 - Depend on organs and imaging modality
 - CT, MR, US, X-Ray, PET,
 - Brain, heart, lung, prostate, ...
 - **Need information about normal cases**
 - **Understanding of abnormal changes**



Bone (1000)

Hemorrhage

(65~95)

GM & WM

 $(20 \sim 40)$

CSF (0)

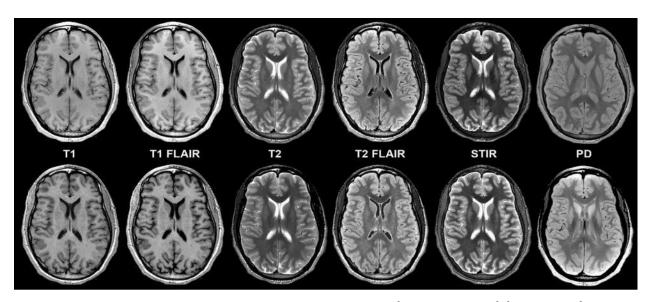
Air (-1000)

Fat (-30~-100)





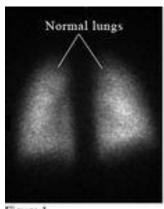
Various Representations of Brain in MRI



- Large variations across patients, imaging device, and hospital
- Difficult to define anomalies and image dissimilarity
 - Data-driven approaches may be promising



- Aims to automatically localize anomalies and quantify their differences from other observations (normal cases)
 - Computer-aided anomaly detection
- Three fundamental approaches to anomaly detection
 - Using prior knowledge of anomalies and normality or not



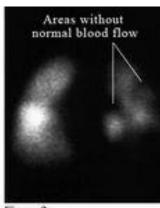


Figure 1 Figure 2

https://www.pinterest.com/pin/108790147231801412/

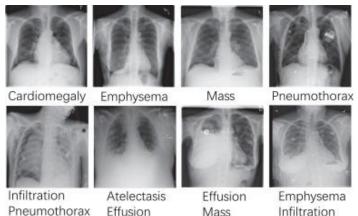
For medical imaging

- Strong or weak annotation by experts
- Regions of interest, landmarks, disease type labels
- Supervised methods
- Unsupervised methods
- 3. Semi-supervised methods

Hodge, V., & Austin, J. (2004). A survey of outlier detection methodologies. *Artificial intelligence review*, 22(2), 85-126.



- Approach #1: with prior knowledge of anomalies and normality
 - Modeling normality and anomalies together
 - Using pre-labelled data
 - Limitations
 - Require a good spread of normal and abnormal data for generalization → not easy in most clinical cases
 - Classification is limited to the known distribution



Pneumothorax Multi-label chest X-Ray image classification

- Using 112,120 chest X-ray images (Chest X-ray14)
- Labelled for 14 disease pathologies + no-finding

^{*} https://www.kaggle.com/nih-chest-xrays/data



- Approach #2: without prior knowledge of training data
 - Assume that abnormal cases are well separated from the normal data
 - Unsupervised clustering methods
 - Remove outliers in training data and fit models to the remaining
 - Use the outliers to build a robust classifier
 - Limitations
 - Difficult to recognize without expertise → machine can do it?
 - Require to define dissimilarity measures between images



(a) "No Finding"



(b) "Cardiomegaly"



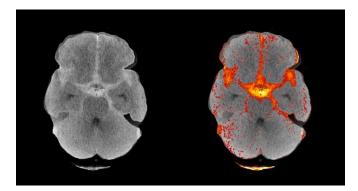
(c) "Pneumothorax"

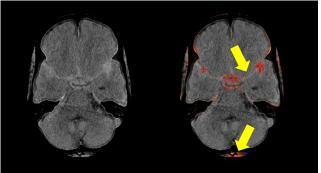


(d) "Pneumothorax"



- Approach #3: modeling normality only
 - Learns to abnormality with supervision about normal class
 - Draw a boundary of normality
 - Suitable when the data set of possible anomalies is limited
 - A way medical doctors recognize lesions in medical images
 - Limitations
 - Lack of prior information on anomalies → high false alarms
 - Require enough samples for normality → how many?





Voxelwise detection using z-score threshold



Challenges in Anomaly Detection

Modeling methods of normal cases

- Representation learning of medical images
 - Curse of dimensionality: 3D/4D volume (CT, MRI), large 2D image (X-Ray)
- Lack of well-defined representative boundary of normal cases

Data collection from healthy subjects

- Good spread of normal cases: represent the diversity of target population
- Factors to consider
 - Age, gender, imaging modality, hospital, and imaging protocol

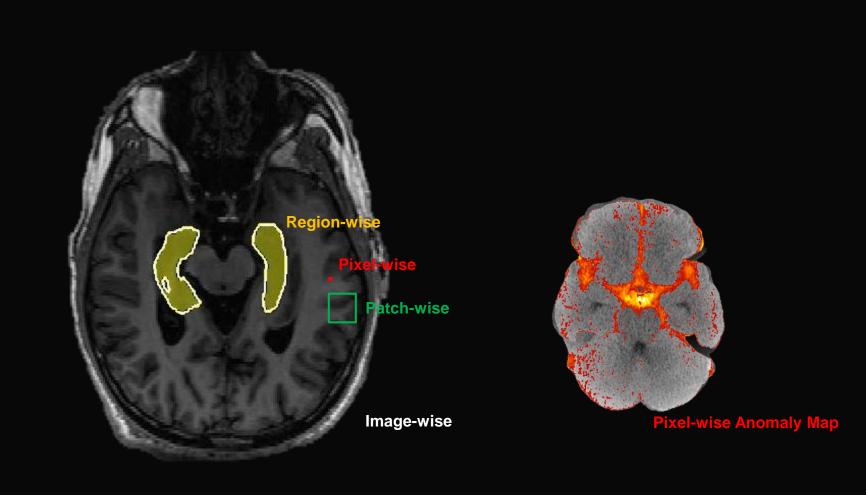
Generalization of models

- How to build more generalized models of normality with limited sample
- Data augmentation, hyperparameter settings, adding noise, ...

Anomaly scores

- Margin from the boundaries of normal cases
- Evaluation: pixel-wise, patch-wise, region-wise, and image-wise





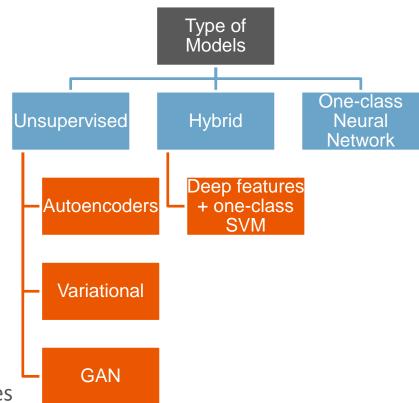


Deep Anomaly Detection



Anomaly Detection using Deep Learning

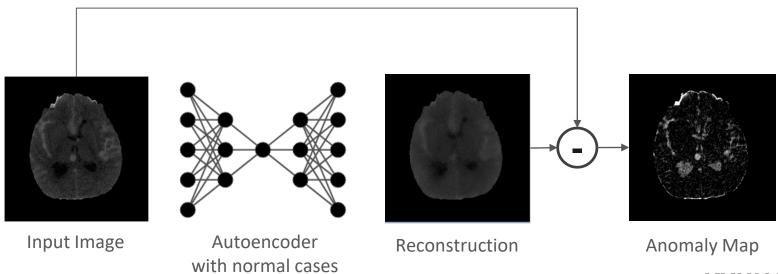
- Models
 - Unsupervised AD
 - Reconstruction-based
 - Hybrid method
 - Classifier using latent representations
 - Classification (one-class)
- Anomaly scores
 - Reconstruction loss
 - Distance from the center of data distribution
 - Depend on models and modalities





Reconstruction-based Anomaly Detection

- Aims to localize anomalies in images
- Assume that anomalies yield higher residuals to the reconstruction of input data
- Deep autoencoders with/without adversarial framework



Autoencoder Approaches

- Robust deep autoencoder
- Deep autoencoding Gaussian mixture model
- Adversarial autoencoder

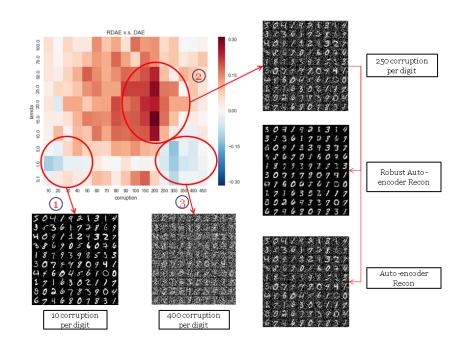


Robust Deep Autoencoders

- An extension of deep autoencoder
 - To discover high quality, non-linear features while eliminating noise
 - Inspired by Robust PCA
 - Optimization problem

$$\min_{\substack{D,E}} \|X - D(E(X))\| \rightarrow \\ \min_{\substack{\theta,S}} \|L_D - D_{\theta}(E_{\theta}(L_D))\|_2 + \lambda \|S\|_1$$
 (Denoising)
$$\min_{\substack{\theta,S}} \|L_D - D_{\theta}(E_{\theta}(L_D))\|_2 + \lambda \|S\|_{2,1}$$
 (Anomalies in group)

subject to $X - L_D - S = 0$

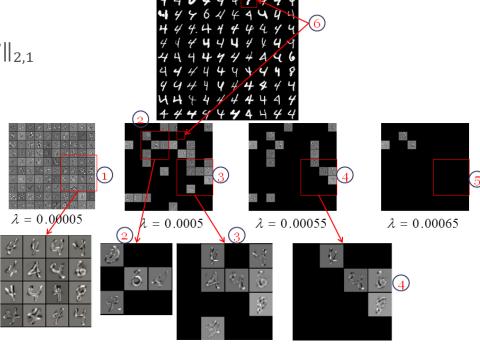


Learning common patterns in data against image noise



Robust Deep Autoencoders

- Anomaly detection
 - S: reconstruction error in $\min_{\theta,S} \|L_D D_{\theta}(E_{\theta}(L_D))\|_2 + \lambda \|S\|_{2,1}$
 - Larger $\lambda \rightarrow$ sparser S
 - $_{\circ}$ Grouped $l_{2,1}$ norm to find abnormal sample
- Working on abnormal sample with significant differences
 - o Anomaly score →pixel-wise error

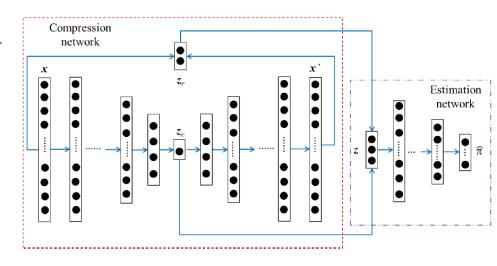




Deep Autoencoding Gaussian Mixture Model

- Curse of dimensionality
 - Any sample could be a rare event with low probability to observe
 - Not easy for density estimation
 - Dimensionality reduction, but key features could be removed
- DAGMM
 - Compression: deep autoencoder
 - Latent features and reconstruction error
 - Estimation: predict the mixture membership for each sample
 - K mixture components

$$E(\mathbf{z}) = -\log \left(\sum_{k=1}^{K} \hat{\phi}_k \frac{\exp\left(-\frac{1}{2}(\mathbf{z} - \hat{\mu}_k)^T \hat{\boldsymbol{\Sigma}}_k^{-1} (\mathbf{z} - \hat{\mu}_k)\right)}{\sqrt{|2\pi \hat{\boldsymbol{\Sigma}}_k|}} \right)$$

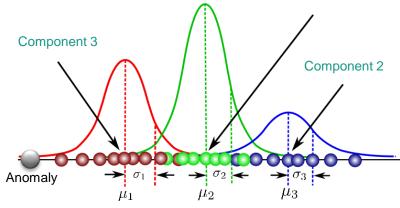


Zong, Bo, Qi Song, Martin Renqiang Min, Wei Cheng, Cristian Lumezanu, Daeki Cho, and Haifeng Chen. "Deep autoencoding gaussian mixture model for unsupervised anomaly detection." (2018).



Deep Autoencoding Gaussian Mixture Model

- Anomaly detection using DAGMM
 - Sample with high energy (E(z))
 - Low likelihood in mixture-component distribution
 - Estimation network considers two features
 - Not only latent representation
 - Also consider reconstruction error
- Anomaly localization
 - How to use the membership information
 - Patch-wise or region-wise evaluation



https://towardsdatascience.com/gaussian -mixture-models-explained-6986aaf5a95

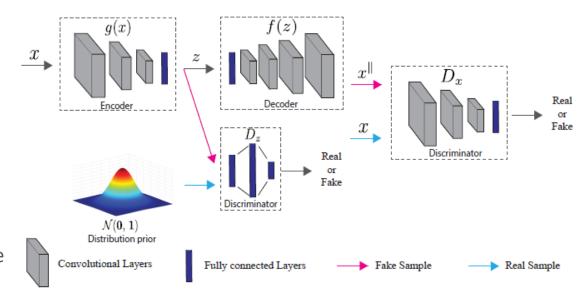
Zong, Bo, Qi Song, Martin Renqiang Min, Wei Cheng, Cristian Lumezanu, Daeki Cho, and Haifeng Chen. "Deep autoencoding gaussian mixture model for unsupervised anomaly detection." (2018).



Component 1

Adversarial Autoencoder

- Learning the probability distribution of normal sample
 - Controlling the latent distribution and image generation
 - To ensure good generative reconstruction of normal sample
- Autoencoder + two discriminators
 - $_{\circ}$ D_z : distinguish btw latent representation and $\mathcal{N}(0,1)$
 - o D_x : distinguish btw the reconstructed image (x') from $\mathcal{N}(0,1)$ and real image

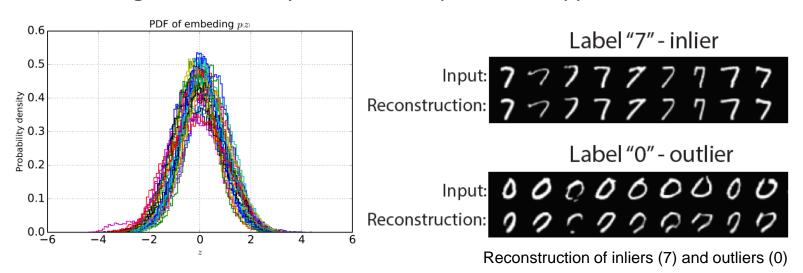


Pidhorskyi, Stanislav, Ranya Almohsen, and Gianfranco Doretto. "Generative probabilistic novelty detection with adversarial autoencoders." In *Advances in Neural Information Processing Systems*, pp. 6822-6833. 2018.



Adversarial Autoencoder

- Anomaly detection
 - By evaluating the inlier probability distribution on test sample
 - Density estimation in latent space
 - o Image-wise anomaly evaluation → patch-wise approach

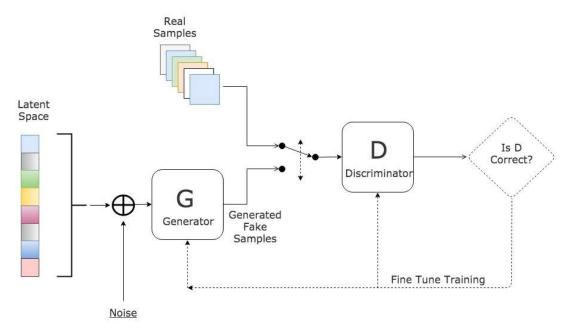


Pidhorskyi, Stanislav, Ranya Almohsen, and Gianfranco Doretto. "Generative probabilistic novelty detection with adversarial autoencoders." In *Advances in Neural Information Processing Systems*, pp. 6822-6833. 2018.



Generative Adversarial Networks

- Deep convolutional GAN (AnoGAN)
- Ganomaly: a GAN for anomaly detection



https://www.kdnuggets.com/2017/01/generative-adversarial-networks-hot-topic-machine-learning.html

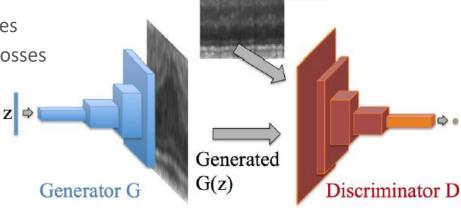


Deep convolutional GAN (AnoGAN)

- Unsupervised learning
 - To create a rich generative model of normal cases
 - Manifold learning of normal anatomical variability
- Mapping images to latent space (z)
 - Latent space search
 - To find the best *z* for normal images
 - Using residual and discrimination losses

$$\mathcal{L}_{R}(\mathbf{z}_{\gamma}) = \sum |\mathbf{x} - G(\mathbf{z}_{\gamma})|$$

$$\mathcal{L}_{D}(\mathbf{z}_{\gamma}) = \sum |\mathbf{f}(\mathbf{x}) - \mathbf{f}(G(\mathbf{z}_{\gamma}))|$$



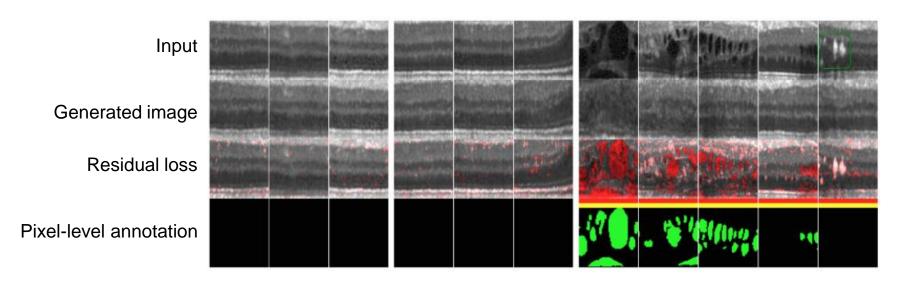
Real

Schlegl, Thomas, Philipp Seeböck, Sebastian M. Waldstein, Ursula Schmidt-Erfurth, and Georg Langs. "Unsupervised anomaly detection with generative adversarial networks to guide marker discovery." In International Conference on 28 Information Processing in Medical Imaging, pp. 146-157. Springer, Cham, 2017.



Deep convolutional GAN (AnoGAN)

- Anomaly detection
 - Anomaly score: $A(\mathbf{x}) = (1 \lambda) \cdot R(\mathbf{x}) + \lambda \cdot D(\mathbf{x})$
 - Pixel-wise residual loss to localize anomalies

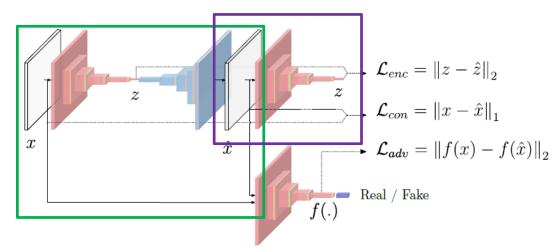


Schlegl, Thomas, Philipp Seeböck, Sebastian M. Waldstein, Ursula Schmidt-Erfurth, and Georg Langs. "Unsupervised anomaly detection with generative adversarial networks to guide marker discovery." In International Conference on 29 Information Processing in Medical Imaging, pp. 146-157. Springer, Cham, 2017.



GANomaly: a GAN for anomaly detection

- Problem of prior GAN based approaches
 - Require latent space search to remap the latent vector to new images
 - Expensive process and high complexity
- GANomaly = encoder-decoder-encoder pipeline
 - To capture the normal data distribution within image and latent space
 - Reconstruction network
 - Adversarial autoencoder (AAE)
 - Latent vector generation
 - Encoder to learn the distributions from a latent space



Akcay, Samet, Amir Atapour-Abarghouei, and Toby P. Breckon. "Ganomaly: Semi-supervised anomaly detection via adversarial training." In *Asian Conference on Computer Vision*, pp. 622-637. Springer, Cham, 2018.

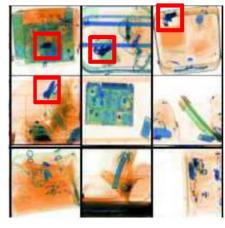


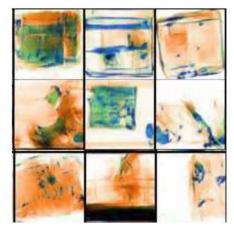
GANomaly: a GAN for anomaly detection

- Anomaly detection
 - Anomaly score = distance between the latent vector of AAE and the inferred vector from the reconstructed image

$$\mathcal{A}(\hat{x}) = \|G_E(\hat{x}) - E(G(\hat{x}))\|_1$$

• \hat{x} : "normal"-like image drawn from the normal data distribution





AAE fails to reconstruct abnormal sample → dissimilarity btw the latent vectors

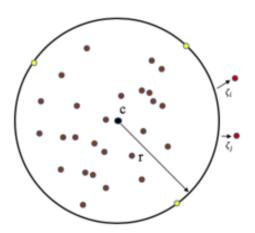
Akcay, Samet, Amir Atapour-Abarghouei, and Toby P. Breckon. "Ganomaly: Semi-supervised anomaly detection via adversarial training." In *Asian Conference on Computer Vision*, pp. 622-637. Springer, Cham, 2018.



FFOB

One-class Classification Methods

- Deep Support Vector Data Description (Deep SVDD)
- One-class Convolutional Neural Network (OC-CNN)
- Adversarially Learned One-Class Classifier for Novelty Detection

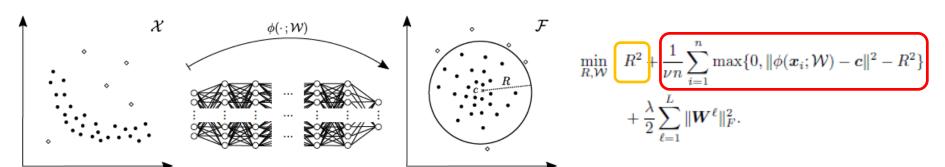


https://en.wikipedia.org/wiki/One-class_classification



Deep Support Vector Data Description

- Previous approaches in one-class classification
 - One-class SVM or kernel density estimation
 - Fails in high-dimensional, data-rich scenarios ← curse of dimensionality
- Deep support vector data description
 - A neural network minimizing the volume of a hypersphere that encloses the latent representations of normality data
 - Learning common features across normal instances



Ruff, Lukas, Robert Vandermeulen, Nico Goernitz, Lucas Deecke, Shoaib Ahmed Siddiqui, Alexander Binder, Emmanuel Müller, and Marius Kloft. "Deep one-class classification." In *International conference on machine learning*, pp. 4393-4402. 2018.

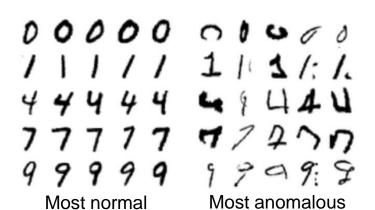


Deep Support Vector Data Description

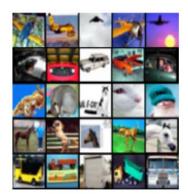
- Anomaly detection
 - Anomaly score = distance of the latent representation of new image to the center of the hypersphere

$$s(\boldsymbol{x}) = \|\phi(\boldsymbol{x}; \mathcal{W}^*) - \boldsymbol{c}\|^2$$

Image-, patch-, and region-wise evaluation → rough localization







Most normal

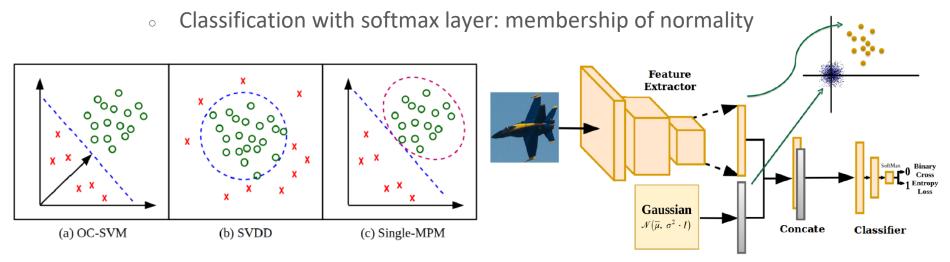
Most anomalous

Ruff, Lukas, Robert Vandermeulen, Nico Goernitz, Lucas Deecke, Shoaib Ahmed Siddiqui, Alexander Binder, Emmanuel Müller, and Marius Kloft. "Deep one-class 34 classification." In *International conference on machine learning*, pp. 4393-4402. 2018.



One-class Convolutional Neural Network

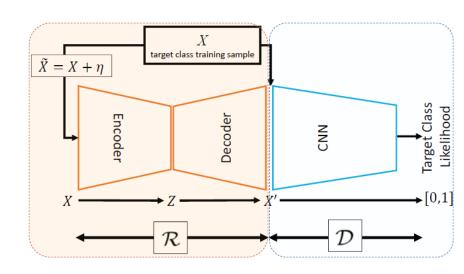
- One-class classifier
 - Mapping image features distant from pseudo-negative data
 - Pseudo-negative data drawn from a Gaussian distribution
- Anomaly detection

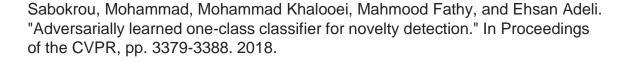




Adversarially Learned One-Class Classifier

- Two networks with adversarial learning
 - \circ Generator (\mathcal{R}): reconstruction from the normal data distribution
 - Discriminator (\mathcal{D}):classification for inliers and outliers
- Using discriminator for anomaly detection
- Input with random noise
 - Robust to image noise and distortions
 - Generalization

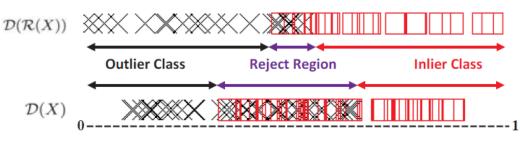






Adversarially Learned One-Class Classifier

- Anomaly detection
 - Using target class likelihood of reconstructed images
 - Simple threshold
 - Low probability → outlier
 - Generator usually fails to reconstruct outlier images





Sabokrou, Mohammad, Mohammad Khalooei, Mahmood Fathy, and Ehsan Adeli. "Adversarially learned one-class classifier for novelty detection." In Proceedings of the CVPR, pp. 3379-3388. 2018.



Deep Anomaly Detection for Medical Image Analysis



Anomaly Detection in Medical Images

- Autoencoder approaches
 - Aims to localize anomalies in medical images
 - \circ Reconstruction errors \rightarrow pixel-wise anomaly score
 - Using variational autoencoder and its variants for manifold learning
- Imaging domains
 - Optical coherence tomography (OCT): retinal disease
 - MRI, CT: brain tumor, brain hemorrhage
 - Diffusion MRI: multiple sclerosis
 - Neural networks designed for specific imaging modalities
- Anomaly scores



Anomaly Score using Variational Autoencoder Gradients

- Prior approaches
 - Reconstruction error as anomaly score
 - Assumption: models fail to reproduce anomalies not seen during training
- Anomaly score with gradients
 - Score = directions towards the normal data samples
 - Magnitude of the score = magnitude of abnormality
 - Score is the derivative of the error function w.r.t the input data

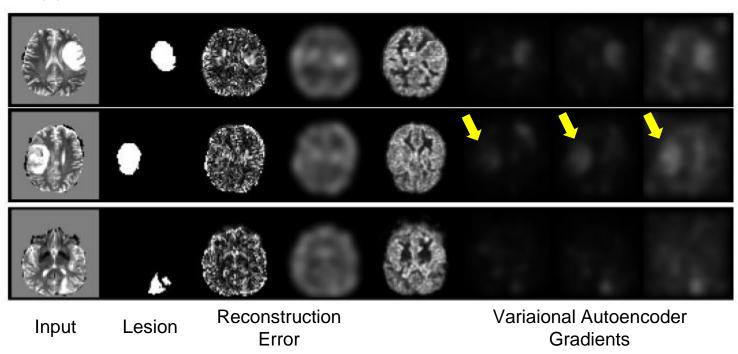
$$\frac{\partial \log p(x)}{\partial x} \approx \frac{\partial (-D_{KL}(q(z|x)||p(z)) + \mathbb{E}_{q(z|x)}[\log p(x|z)])}{\partial x}$$

Zimmerer, David, Jens Petersen, Simon AA Kohl, and Klaus H. Maier-Hein. "A Case for the Score: Identifying Image Anomalies using Variational Autoencoder Gradients." *arXiv preprint arXiv:1912.00003* (2019).



Anomaly Score using Variational Autoencoder Gradients

Application to brain MR



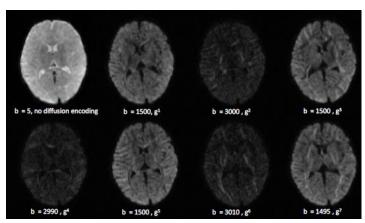
Zimmerer, David, Jens Petersen, Simon AA Kohl, and Klaus H. Maier-Hein. "A Case for the Score: Identifying Image Anomalies using Variational Autoencoder Gradients." *arXiv preprint arXiv:1912.00003* (2019).

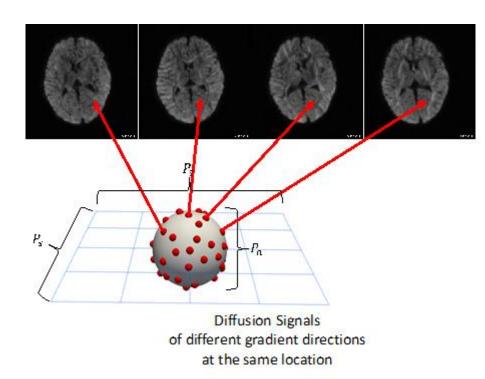


q-Space Novelty Detection with Variational Autoencoders

Diffusion MRI

- Mapping the diffusion process
 of water molecules
- Multiple volumes with different b-values and gradient directions

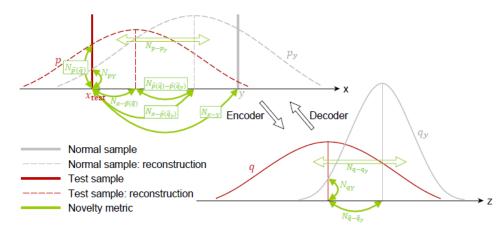






q-Space Novelty Detection with Variational Autoencoders

- Input feature
 - d-dimensional vector of diffusion directions
 - Voxel-wise modeling
- Normality modeling: Variational autoencoder
- Various anomaly scores
 - Deterministic error
 - Stochastic error
 - Multiple inference
 - Average and min error
 - Distance btw latent feature

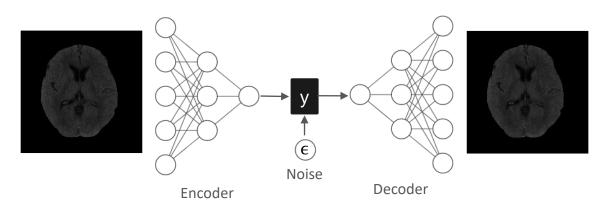


Vasilev, Aleksei, Vladimir Golkov, Marc Meissner, Ilona Lipp, Eleonora Sgarlata, Valentina Tomassini, Derek K. Jones, and Daniel Cremers. "q-Space Novelty Detection with Variational Autoencoders." arXiv preprint arXiv:1806.02997 (2018).



Uncertainty Autoencoder for Anomaly Detection

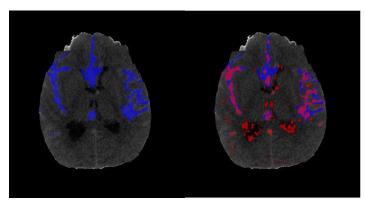
- Limitations of variational autoencoder
 - To regularize the latent space to follow normal distribution → difficult to model normal data distribution
- Spatial Uncertainty Auto-encoder
 - Add isotropic Gaussian noise to model the data distribution as Gaussian with fixed scalar variance
 - Spatial autoencoder to preserve anatomical features of brain images
 - Reconstruct "normal-like" brain image for disease cases





#4. Reconstruction-based Anomaly Detection

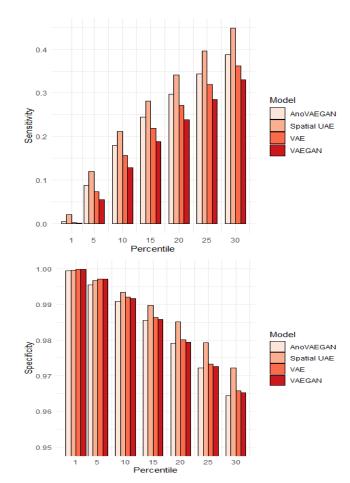
Application to brain hemorrhage



 Better sensitivity compared to VAE, VAE-GAN

Grover, A., & Ermon, S. (2018). Uncertainty autoencoders: Learning compressed representations via variational information maximization. *arXiv* preprint *arXiv*:1812.10539.

Jaeil Kim, et al. Unsupervised anomaly detection in brain CT, in preparation

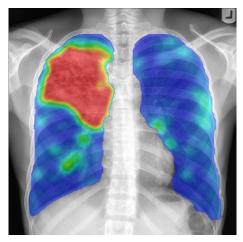


Summary



Summary

- Deep anomaly detection methods
 - Autoencoder approaches
 - Generative adversarial networks
 - One-class classification
- Open questions
 - How to reduce false positives and false negatives
 - Large variations across subjects and image quality
 - "Normal"-like reconstruction process
 - Reconstruction of abnormal region is unpredictable
 - Anomaly evaluation: image-wise, patch-wise, pixel-wise
 - Limited number of sample from normal cases
 - Generalization matters
 - Clinical interpretation of anomaly scores
 - how images are separated from normal cases



https://medium.com/analytics -vidhya/detecting-anomaliesin-x-ray-using-cnn-1e4c2e49f23a



Discussion

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